## UPPSALA UNIVERSITET

Matematiska institutionen Erik Palmgren

EXERCISES
BONUS PROBLEMS 3
APPLIED LOGIC
2009-09-28

## Type theory. Gödel-Gentzen negative translation.

CLTT refers to the March 2004 version of the handout *Constructive Logic and Type Theory*, by Erik Palmgren. (Available on the webpage of the course.) The BONUS PROBLEMS are marked (+) below. Your solutions of these are to be presented at the blackboard October 2. Maximum bonus for this set is 2.5%.

- 1. (+) Exercise 7.1 (e), (f) in CLTT.
- 2. (+) Translate the formula

$$(\forall x \in D) (A(x) \land B(x)) \rightarrow (\forall x \in D) A(x) \land (\forall x \in D) B(x)$$

into a type of Martin-Löf type theory, using the propositions-as-types principle. Prove it to contain an element.

- 3. (+) Exercise 7.3 in CLTT. Compare your result with what is automatically generated by Coq.
- 4. (+) Exercise 6.1 in CLTT.
- 5. Exercise 6.2 (c), (e) in CLTT.
- 6. (+) \* Exercise 6.4 in CLTT