

Convergence of Fourier series I

What do the main theorems say?

Theorem 4.5.4

If $A = \frac{1}{2} \lim_{s \rightarrow 0} (f(t+s) + f(t-s))$ exists and **if** the Fourier series converges, then $A = f$. series

The theorem does not say that the F. series converges!!

Theorem 4.5.5

If $\sum_{n \neq 0} |f(n)| < \infty$ (*)

then

$$f(t) = \sum_{n \neq 0} \hat{f}(n) e^{int}$$

almost everywhere, in particular at points where $f(t)$ is continuous.

Provides a criterion (*) for a continuous $f = f$. series

Theorem 4.8.2

If the left and right limit values $f(t_-)$ and $f(t_+)$, and left/right derivatives $f'(t_-)$, $f'(t_+)$ exist, then F.s. converges and is equal to f .

A criterion for convergence and equality $f = \sum \dots$

Theorem 4.8.3

If f is Hölder continuous, then F. series converges and is equal to f .

Provides a criterion for $f = f$. series: Hölder continuity.