

Fouriertransformen

$$f(t) \xrightarrow{\mathcal{F}} \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt = \hat{f}(\omega)$$

Transformregler

	$f(t)$	$\hat{f}(\omega)$
Lineäritet	$\alpha f_1(t) + \beta f_2(t)$	$\alpha \hat{f}_1(\omega) + \beta \hat{f}_2(\omega)$
t -derivering	$f'(t)$	$i\omega \hat{f}(\omega)$
ω -derivering	$-it f(t)$	$\frac{d\hat{f}(\omega)}{d\omega}$
t -translation	$f(t - t_0)$	$e^{-i\omega t_0} \hat{f}(\omega)$
ω -translation	$e^{it\omega_0} f(t)$	$\hat{f}(\omega - \omega_0)$
Skalning	$f(at), a \neq 0$	$\frac{1}{ a } \hat{f}\left(\frac{\omega}{a}\right)$
	$f(-t)$	$\hat{f}(-\omega)$
Symmetri	$\hat{f}(t)$	$2\pi f(-\omega)$
Faltning	$\int_{-\infty}^{\infty} f(u) g(t - u) du$	$\hat{f}(\omega) \hat{g}(\omega)$

Speciella transformpar

$\delta(t)$	1
$\Pi_{-\frac{1}{2}, \frac{1}{2}}(t)$	$\text{sinc}\left(\frac{\omega}{2}\right) = \frac{\sin\left(\frac{\omega}{2}\right)}{\frac{\omega}{2}}$
$\Lambda_{-1,1}(t)$	$\text{sinc}^2\left(\frac{\omega}{2}\right) = \frac{\sin^2\left(\frac{\omega}{2}\right)}{\left(\frac{\omega}{2}\right)^2}$
$e^{- t }$	$\frac{2}{\omega^2 + 1}$
$e^{-t} \theta(t)$	$\frac{1}{i\omega + 1} = \frac{1}{\omega^2 + 1} - \frac{i\omega}{\omega^2 + 1}$
$e^{-\frac{t^2}{2}}$	$e^{-\frac{\omega^2}{2}} \sqrt{2\pi}$

Plancharels formler

$$\int_{-\infty}^{\infty} |f(t)|^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} |\hat{f}(\omega)|^2 d\omega \qquad \int_{-\infty}^{\infty} f(t) \overline{g(t)} dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} \hat{f}(\omega) \overline{\hat{g}(\omega)} d\omega$$